

# Enhanced Location Estimation via Pattern Matching and Motion Modeling

*Harald Kunczler, [kunczler@ftw.at](mailto:kunczler@ftw.at)  
ISART 2004, Boulder*

- Motivation
- Signal Power Level localization method
- Motion model
- Trial and Results
- Conclusions

# Measurement Sites (GPS)

Area Type	Inaccuracy	Availability
“Ring”	<~23meter	~85%
“Downtown”	<~50meter	~57%



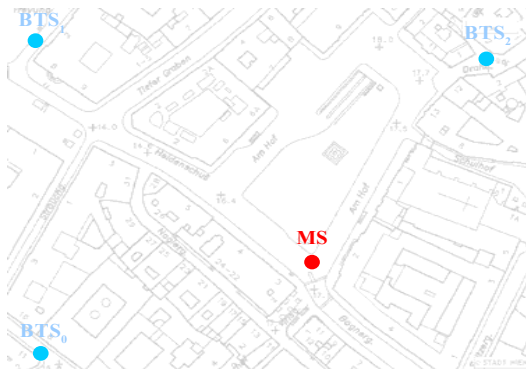
Area  
“Downtown”:

Area “Ring”:

# Power Level bases Loc. Methods

**Localize handset by „unique“ RF pattern!**

Extract feature vector:

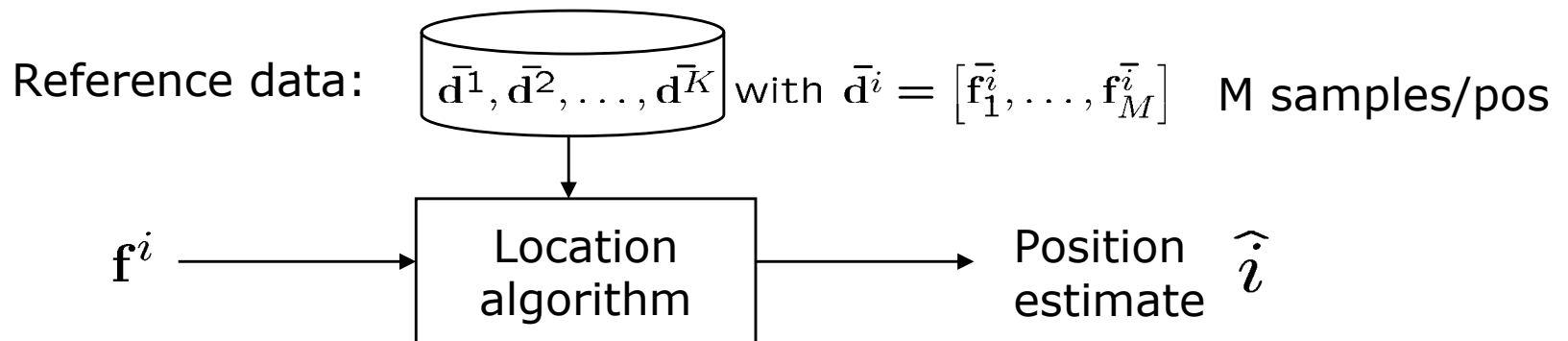


Single position  $i$ :

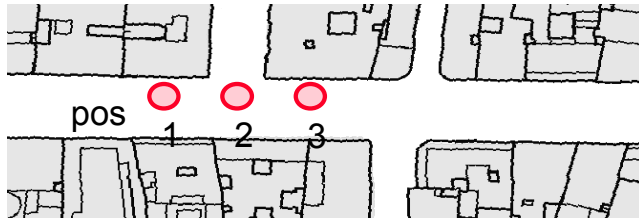
$$\mathbf{f}^i = \begin{bmatrix} a_0^i & a_1^i & \dots & a_6^i \end{bmatrix}$$

- $a$  ... Cell ID
- Index 0: ... Serving cell
- Index 1 to 6: ... Neighboring cells

Compare with reference data:



# Method continued

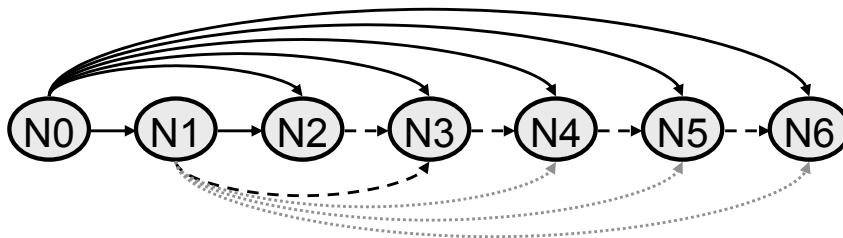


Assign model  $\lambda$  to every position:

$$\lambda^i \iff \text{pos } i$$

Model  $\lambda^i$ : represents all reference data  $d^i$  at position  $i$

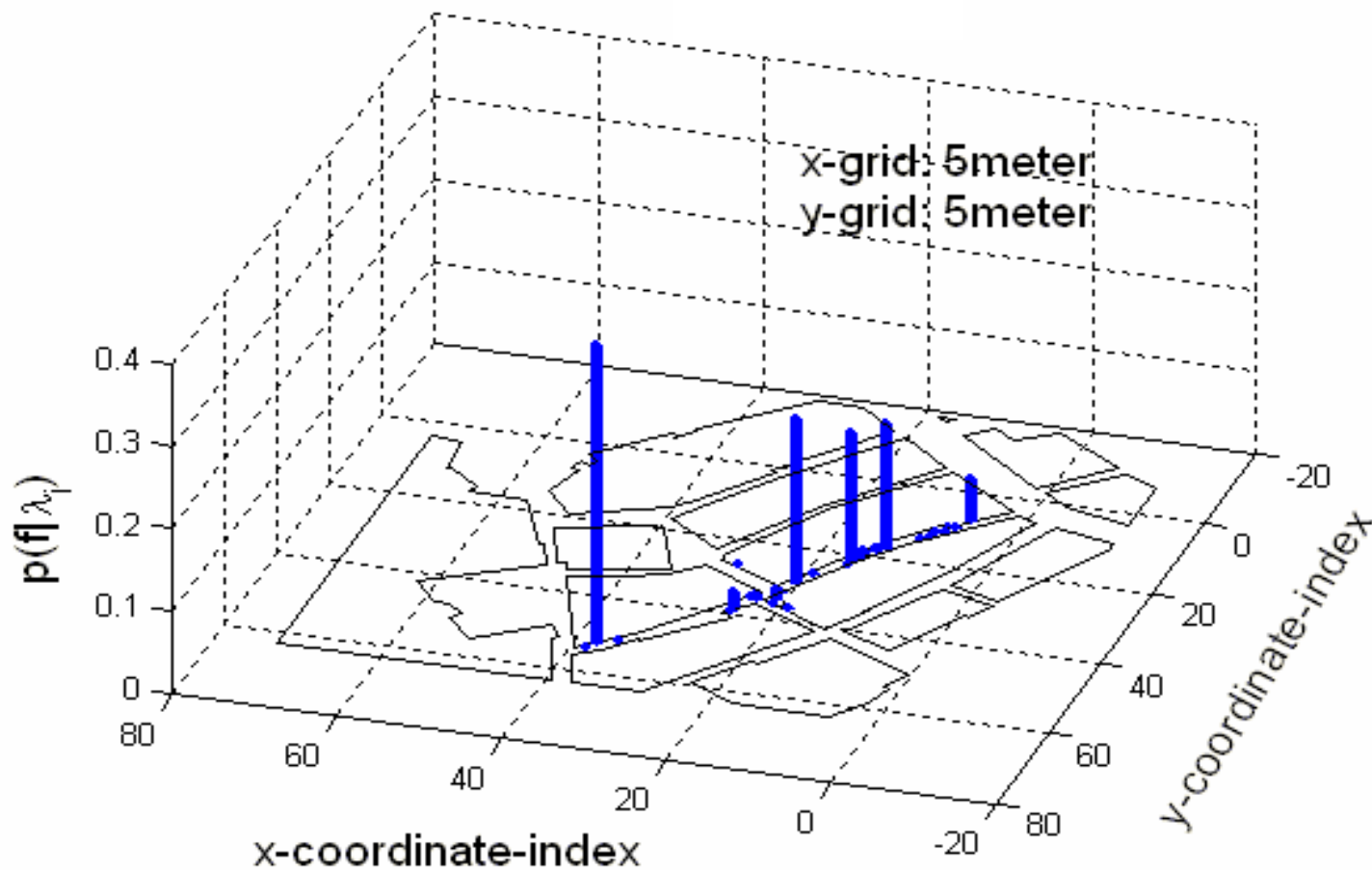
- use non parametric models
- Used prior information (of neighboring positions)
- Use incomplete alphabet of nodes to decrease cardinality



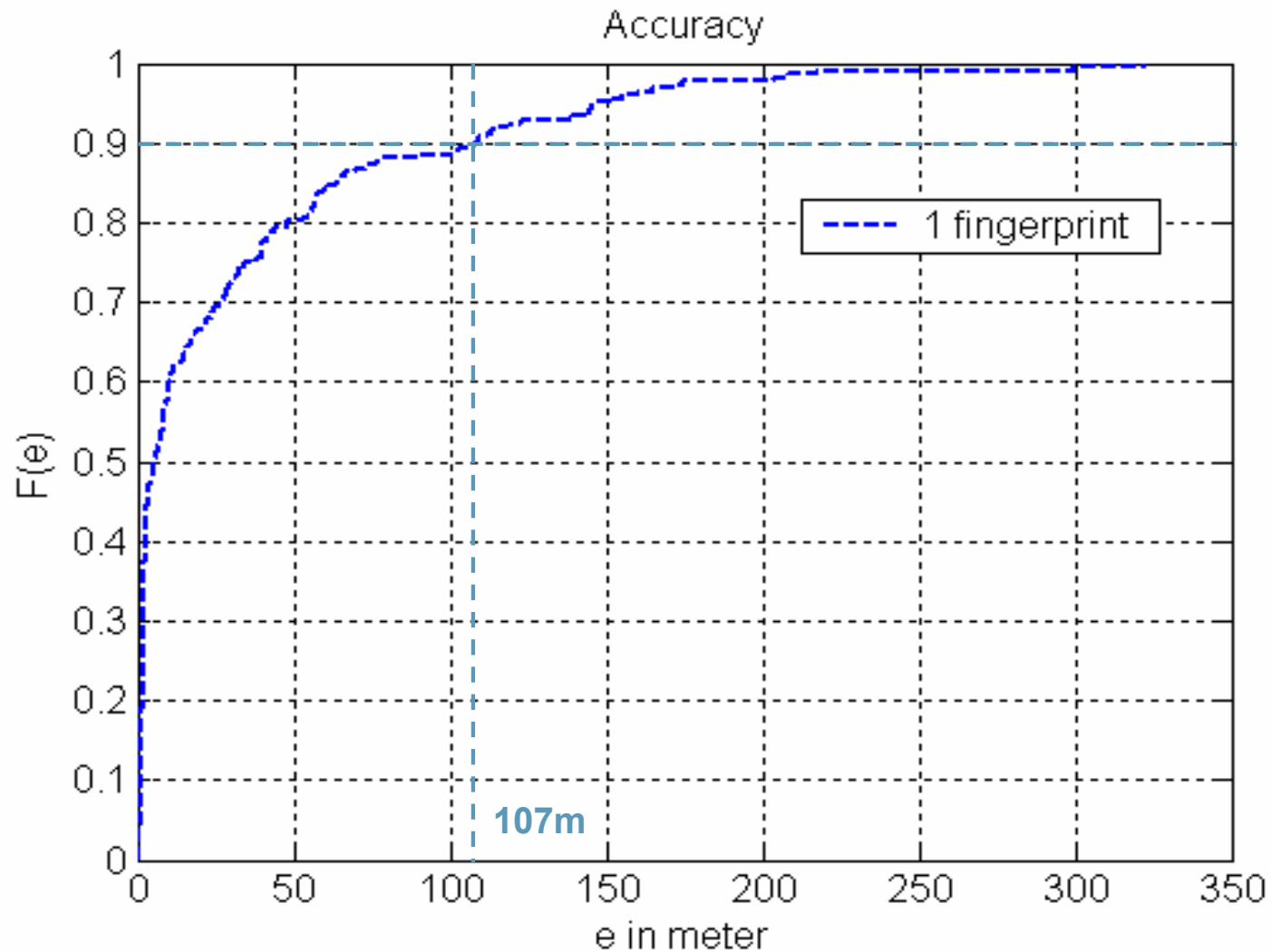
N0: Serving Cell  
N1-N6: Neighboring cells

# Likelihood of Position $i$

Localization: Find the model  $\lambda^i$  and thus  $i$ ) which emits most likely the measured fingerprint  $f^i$



# Accuracy in Urban Areas

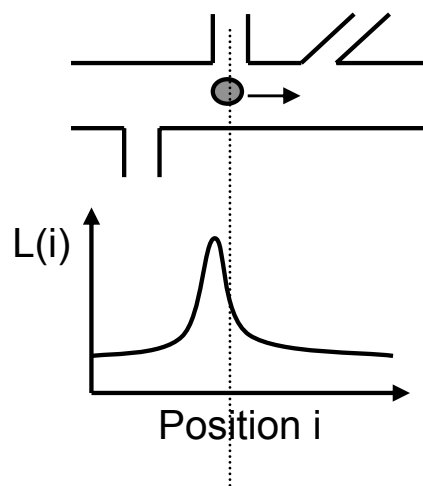


2800 test cases, uniformly distributed within target area

# Utilization of Several Fingerprints

Step 1:

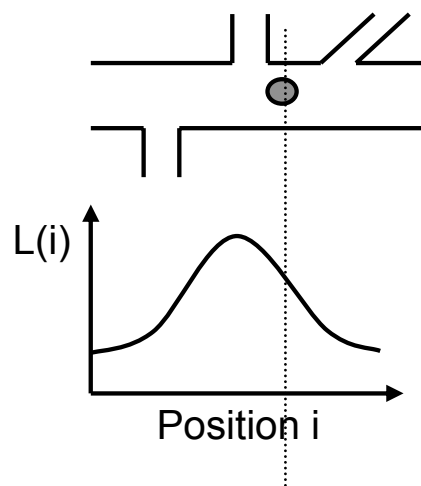
time  $t = k$



First  
position  
estimate

Step 2:

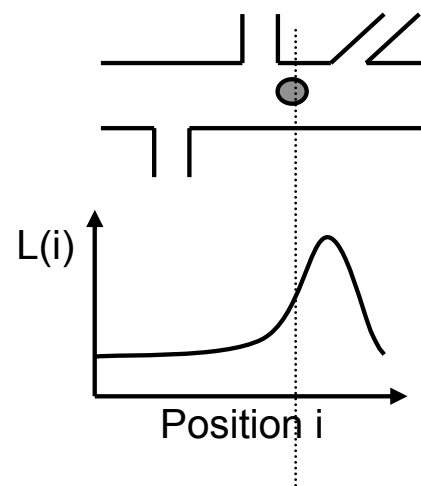
time  $t = k+1$



Propagated  
position  
estimate

Step 3:

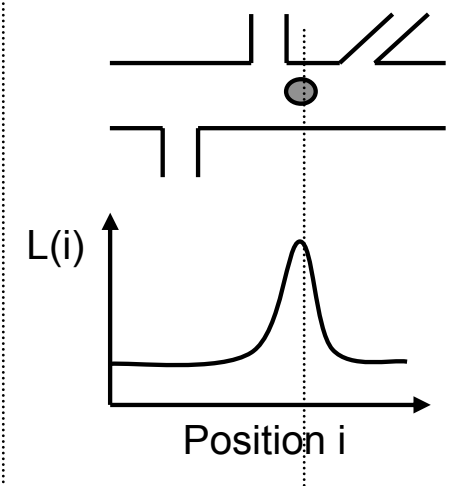
time  $t = k+1$



Second  
position  
estimate

Step 4:

time  $t = k+1$



Combined first and  
second position  
estimate



# Motion Model (based on [1])

- Constant velocity for the time under consideration
- Obstacles are viewed as perturbations upon the constant velocity
- Users try to reestablish their constant velocity

Use state space model:

$$\dot{x}(t) = v(t) + u(t)$$

$$\dot{v}(t) = -\alpha v(t) + w(t)$$

$x(t)$  ... covered distance

$v(t)$  ... user's velocity variation

$u(t)$  ... user's desired velocity

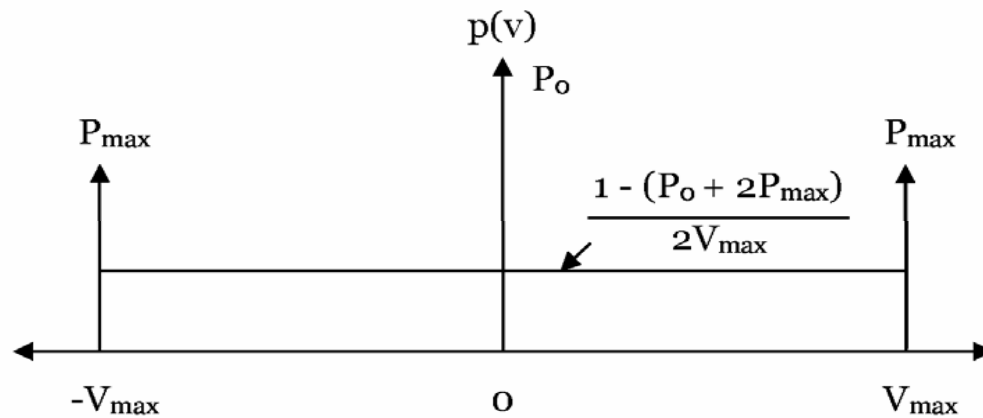
$w(t)$  ... white Gaussian noise

$\alpha$  ... reciprocal velocity time constant

[1] D. Helbing, "A mathematical model for the behavior of pedestrians," *Behavioral Science*, vol. 36, pp. 298–310, 1991.

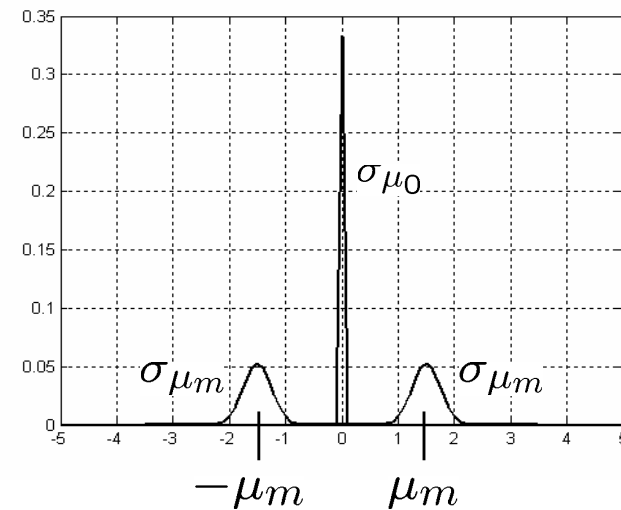
# Density Assumptions

Assumed probability density  
of velocity variation  $v$



$V_{max}$  ... max. speed increase  
 $P_0$  ... probability of no perturbation  
 $P_{max}$  ... probability of max. speed increase

Assumed probability density  
of velocity  $u$



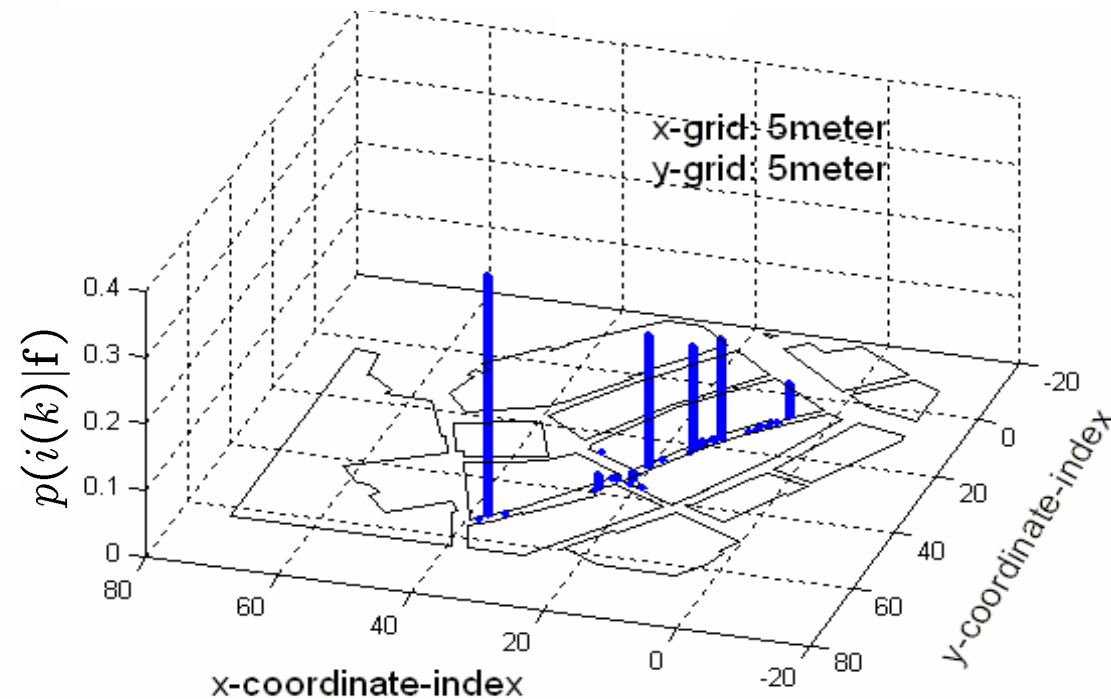
$\mu_m$  ... mean velocity of moving user  
 $\sigma_{\mu_m}^2$  ... variance of moving user  
 $\sigma_{\mu_0}^2$  ... variance of motionless user

# Propagation of Position Estimate

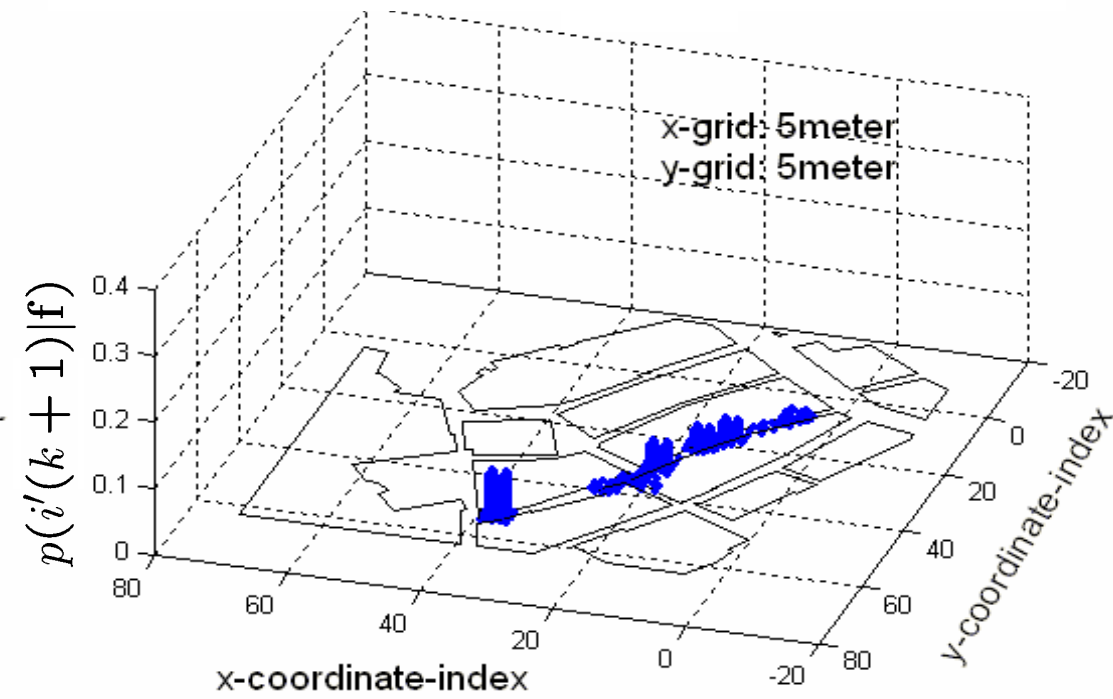
$\mathcal{L}(i) \propto p(i) \quad \dots$  if no prior belief about  $p(\mathbf{f})$  and  $p(i)$

$i'(k + 1) = i(k) + x(k + 1)$  ← motion model's contribution  
 ← position estimate at time k

Probability of being at position  $i$  at time  $k$



Probability of being at position  $i'$  at time  $k+1$



# Combination of Position Estimates



new combined  
estimate

propagated  
estimate

new estimate  
at time  $k+1$

$$i^*(k + 1) = (I - K)i'(k + 1) + Ki(k + 1)$$

$K$  ... Blending Factor

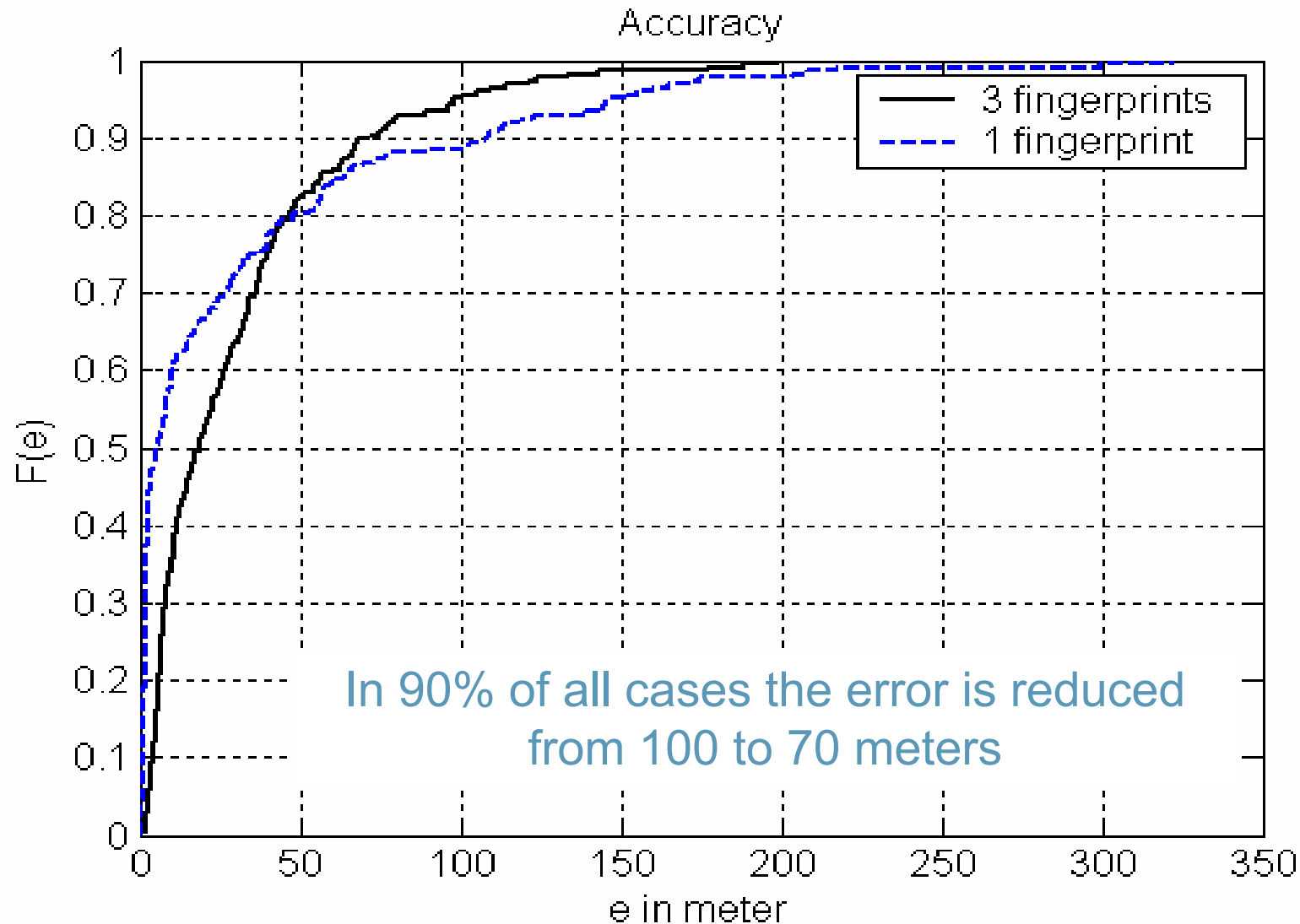
$I$  ... Identity Matrix

- $K$  is found by minimizing the variance of the estimator
- $K$  can be computed in closed form

# Test Area



# Accuracy (3 Fingerprints)



2800 test cases, uniformly distributed within target area

- Pro:**
- 100% availability (GPS less than 60% in downtown of Vienna)
  - Accuracy upper bounded by cell size.
  - Suitable for urban areas.

- Con:**
- Reference data (still) necessary
  - Weak for indoor environments (but can be combined with other methods)

Thank you!